

## Session I: Compositionality and Saturation

### 1. Truth-Conditions & Compositionality

- The Meaning of Sentences

- (1) a. The capital of Burkina Faso is Ouagadougou.  
b. The capital of Burkina Faso is Niamey.

→ Part of the meaning of sentences is whether they are true or false when interpreted relative to particular situations or utterance contexts.

→ We say that a sentence is true ('1') or false ('2') relative to a situation S. For the examples in (1ab), we can write this as follows, if we take 'S1' to stand for our actual world as evaluation world/situation.

- (2) a.  $[[ (1a) ] ]^{S1} = 1$   
b.  $[[ (1b) ] ]^{S1} = 0$

BUT: This cannot be all since...

i. The truth value of sentences can change over time / or situations:

- (3) a. Malte is in Ghana → may be true or not depending on the circumstances  
b. The cat is on the mat. → is true when interpreted relative to situation S35:

S35:



ii. We can grasp the meaning of a clause without knowing whether it is true or not.

- (4) a. Ouagadougou has more than 1 Mio. inhabitants.  
b. The river Nile is longer than 1500 kms.  
c. The French president is in Paris right now.

iii. Sentences with identical truth value mean different things nonetheless:

- (5) a. Water boils at 100°C temperature under normal conditions ≠  
b. Cats are mammals.

- Cresswell (1978): "What I want to put forward as the semantic competence of a speaker is *nothing more or less than his ability, when presented with a sentence and a situation, to tell whether the sentence, in that situation is true or false.*"

→ A sentence  $\alpha$  is true relative to a given evaluation situation S if and only if the **truth conditions** of  $\alpha$  are satisfied in S

→ To know the meaning of a sentence is to know its **truth conditions** (Tarski 1944)

- **Productivity/Creativity and Compositionality**

i. *Observation I:*

As native speakers of a language, we can produce and interpret utterances of arbitrary length and complexity even if we have never uttered or heard them before:

- (6) Ezeulu rose from his goatskin and moved to the household shrine on a flat board behind the central dwarf wall at the entrance.

ii. *Observation II:*

The interpretation of a sentence depends on its syntactic structure.

- (7) a. Cats eat mice.  
 b. Mice eat cats.

- (8) a. Audu yaa ga Musa. (HAUSA, CHADIC)  
 'Audu sees/saw Musa.'  
 b. Musa yaa ga Audu.  
 'Musa sees/saw Audu.'

*Principle of Compositionality* (Frege 1879, Heim & Kratzer 1998: ch.1):

The meaning of a clause, i.e. its truth conditions, depends in a systematic way on the meaning of its parts and the way in which they are syntactically combined

→ ***truth-conditional compositional semantics***

## 2. Saturation by Functional Application: Functions and Arguments

**Q:** How to determine the truth conditions of clauses in compositional fashion ?

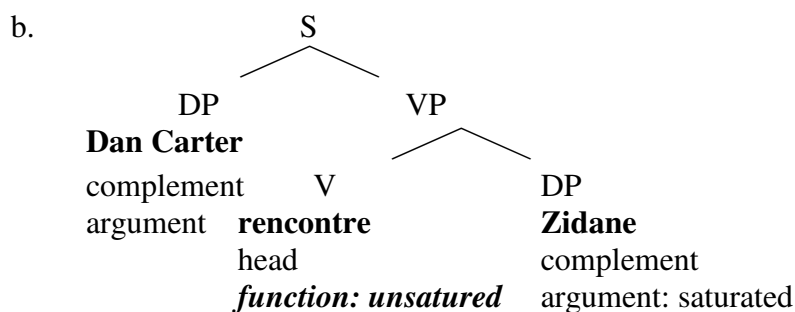
- *Frege's Central Insight:*

Different parts of a sentence play different roles in the derivation of its meaning.

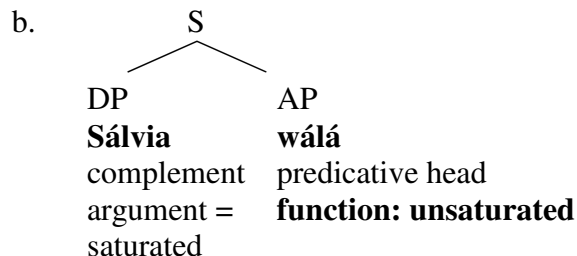
- (9) a. predicative expressions (V, A, P, bare Ns): ***unsaturated, semantic functions***  
 b. nominal arguments (DPs): ***saturated, semantic arguments***

→ Typically, though not obligatorily, there is a tight connection between syntactic *head-complement* structure and semantic *function-argument* structure.

- (10) a. Dan Carter *rencontre* Zidane.  
 Dan Carter met Zidane



- (11) a. Sálvía wálá. (BURA, CENTRAL CHADIC)  
 Sálvía big/important  
 ‘Sálvía is big/important.’



→ the same combinatory logic applies to head-complement combinations of P+DP → PP  
 (in the house), Det+NP → DP (the house), etc.

• *Conclusion:*

A major mechanism of deriving sentence interpretations in a compositional way consists in applying the meaning of unsaturated, or **function-denoting**, expressions to the meaning of their saturated arguments, until all argument positions are saturated.

= **Function Application**

- (12) [[ Dan Carter rencontre Zidane ]] = [[S]]  
 = [[VP]] ([[DP<sub>Subj</sub>]])  
 = ([[V]] ([[DP<sub>Obj</sub>]]) ([[DP<sub>Subj</sub>]])  
 = ([[rencontre]])(zidane)(dan carter)

→ The interpretation of a sentence with a transitive verbs and its two syntactic complements involves two instances of function application where the order of semantic arguments is determined by syntactic structure.

**Ex.1** How is the meaning of the predicative construction in (11) derived?

### 3. Technicalities: $\lambda$ -Calculus (Heim & Kratzer 1998: 34-40)

**Q:** How can we formally represent the unsaturated function meaning of predicative expressions in natural language?

- the  $\lambda$ -calculus allows for a short and concise formal notation of the meaning of function-denoting expressions and of the application of these function-denoting expressions to their saturated semantic arguments:

- (13) a. [[laugh]] =  $\lambda x \in D_e. x \text{ laughs}$   
 READ: the meaning of *laugh* is a function that takes individuals  $x$  of type  $e$  (=entity) as its sole argument and maps them to the truth value ‘1’ if and only if  $x$  has the property of laughing in the relevant situation
- b. [[important]] =  $\lambda x \in D_e. x \text{ is important}$
- c. [[rencontrer]] =  $\lambda x \in D_e. \lambda y \in D_e. y \text{ meets } x$

- **Conventions of the  $\lambda$ -calculus**

- (14) i. each  $\lambda$  stands for a function that applies to arguments in its domain and maps them onto function value.
- ii. Any variables ( $x, y, P, \dots$ ) bound by a  $\lambda$ -operator to the left of the full stop stand for argument positions to be satisfied by arguments from within the function domain.
- iii. the expression to the right of the full stop stands for the function value after function application to the argument
- iv. if function application yields a truth value (i.e. at the sentence-level), we do not write  $\lambda$ ,  $\lambda$  or  $\lambda$ , but specify the relevant truth conditions instead.
- RULE OF THUMB:  $\lambda$ -terms stand for the meaning of unsaturated, function-denoting expressions.

- **Function application as  $\lambda$ -conversion**

- We have already seen that the semantic interpretation of many sentences proceeds in a compositional fashion by function application of unsaturated expressions (predicates → functions) to saturated arguments of appropriate kind.
- the  $\lambda$ -calculus provides an easy technical means of modelling the semantic composition procedure of function application:  *$\lambda$ -conversion*

(15)  $\lambda$ -conversion (schematically):

- i. combine the  $\lambda$ -term (a function) and its argument(s) by writing the argument in round brackets behind the  $\lambda$ -term in square brackets:
- a.  $[\lambda x. P(x)] (z)$
- ii. The result of function application is obtained by deleting the  $\lambda$ -operator and the variable to the left of the full stop (here:  $\lambda x$ ) and by replacing the variable in the function value (here:  $x$ ) by the concrete value of the argument (here:  $z$ )
- b.  $P(z)$

(16) *general scheme of  $\lambda$ -conversion*:

$$[\lambda x. P(x)] (z) \Leftrightarrow P(z)$$

- iii. in case of multiply unsaturated functions, the arguments appear in left-to-right order in the order of application, i.e. inner arguments before outer arguments, and the  $\lambda$ -operators are deleted from left to right:

$$\begin{aligned} (17) \quad & [\lambda x. \lambda y. R(y)(x)] (u)(v) \\ \Leftrightarrow & [\lambda y. R(y)(u)] (v) \\ \Leftrightarrow & R(v)(u) \end{aligned}$$

- **Sample derivation:**

(18)  $[[ \text{Dan Carter rencontre Zidane } ]]$  = ?

- (19) a.  $[[\text{Dan Carter rencontre Zidane}]] = ([[\text{rencontre}]]) (\text{zidane})(\text{dan carter})$   
 b.  $= [\lambda x \in D_e. \lambda y \in D_e. y \text{ meets } x] (\text{zidane})(\text{dan carter})$   
 c.  $= [\lambda y \in D_e. y \text{ meets Zidane}] (\text{dan carter})$   
 d.  $= 1$  iff Dan Carter meets Zidane.

**Ex.2** How is the meaning of the predicative construction in (11) derived by means of  $\lambda$ -calculus and  $\lambda$ -conversion?

#### 4. An apparent problem & two solutions

- *Observation:* In many agglutinating languages (including some Romance languages, Bantu languages, North American languages, and possibly more), it appears that pronominal arguments need not be realized overtly:

→ In such cases, the sentence seems to consist of a verb plus agreement morphology

- (20) a. T-a-híy-u-‘ (LAKHOTA, Baker 1995)  
 cis-fact-1sI/MsII-give-punc  
 I give it to him  
 b. a-ná-mwáápey-átsa (MAKHUWA-ENAHARA, van der Wal 2009)  
 2-pres.dj-cook-plur  
 ‘They are cooking.’

**Q1:** Do these verb-based expressions constitute full-fledged saturated sentences with truth conditions and truth values?

**Q2:** Is this a case of cross-linguistic variation?

TYPE A-LANGUAGES: fully surface compositional = directly compositional

→ functions (head) and arguments (complements): Function Application

→ functions apply in the same way to pronominal and full noun arguments

TYPE B-LANGUAGES: different semantics for *V+pronoun* and *V+full noun*

→ functional meaning plus agreement morphology: ???

→ functions plus arguments with full nominal expressions: Function Application

- *Two possible solutions:*

i. PRO DROP:

- Agreement markers in some B-type languages are indeed agreement markers, but pronominal arguments are not realized overtly, but covertly as *pro*. The overt agreement marker allows for correct resolution of the covert pronoun, cf. (21a).

- (21) a. pro ha comprato una macchina. [ITALIAN]  
 3sg bought a car  
 ‘He/she bought a car.’

- Full nominal arguments function as ordinary arguments and provide the verb meaning with an explicit semantic argument, cf. (21b).

- (21) b. Giovanni ha comprato una macchina. [ITALIAN]  
 John 3sg bought a car  
 'John bought a car.'

ii. PRO-ARG:

- Many North American languages (Lakhota, Mohawk, Strait Salish) have been analysed as *proarg*-languages. The alleged agreement markers on the verb are not agreement markers, but pronominal arguments that incorporate into the verb stem.

- (22) t'əm'-t-Ø = lə' = sən (→ t'əm'tlə'sən) [STRAIT SALISH, Jelinek 1995]  
 hit-TRAN-3ABS PAST 1sNOM  
 'I hit him.'

- Additional full NPs do not function as semantic arguments, but are left-dislocated topics that are coreferential with the respective pronouns under co-indexation

- (23) a. Shawátiš shako-núhwe'-s Uwári  
 John MsI/FsII-like-hab Mary  
 'John likes Mary.'

b. [<sub>S</sub> John [<sub>S</sub> **pro**-likes-**pro**] Mary]

c. ≈ John<sub>1</sub>, he<sub>1</sub> likes her<sub>2</sub>, Mary<sub>2</sub>

- CORRECT PREDICTION: Genuine quantificational NPs, such as *everybody* and *nobody*, are categorically ruled out in *proarg*-languages, presumably for the same reason that blocks the construal of pronouns with left-dislocated quantifiers in Italian or English:

- (24) \*Nessuno, lo conosco in questa città.  
 nobody, him know.1sg in this city  
 \*'Nobody, I know him in this city.'

## 5. Homework Assignment

- Check whether your own language has predicative and transitive structures parallel to (10a) and (11a) above. Give examples.
- Are such sentences interpretable by means of function application? If so, give a sample derivation for a simple clause. If not, what might be possible reasons?
- What is the semantic function, if any, of the copula element *is* in English (25):

(25) The cat *is* black.

- Does your own language have copular elements? If so, check whether they behave like English *is*, or whether they have additional semantic functions.
- Consider the following Hausa sentence with an optional full subject NP:

- (26) (Musa) ya-a tàfi  
 Musa 3SG-PERFleave  
 'Musa / He left.'

- Give two alternative syntactic analyses of (26), treating Hausa (i.) as a *prodrop*-language; and (ii.) as a *proarg*-language.
- How would the semantic derivation proceed on either syntactic analysis (ignore the semantic contribution of the perfective marker *-a*)? In particular, which syntactic expression would provide the verb with its unique argument?

## **Literature**

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